

# Event cameras

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Bucharest Computer Vision Reading Group

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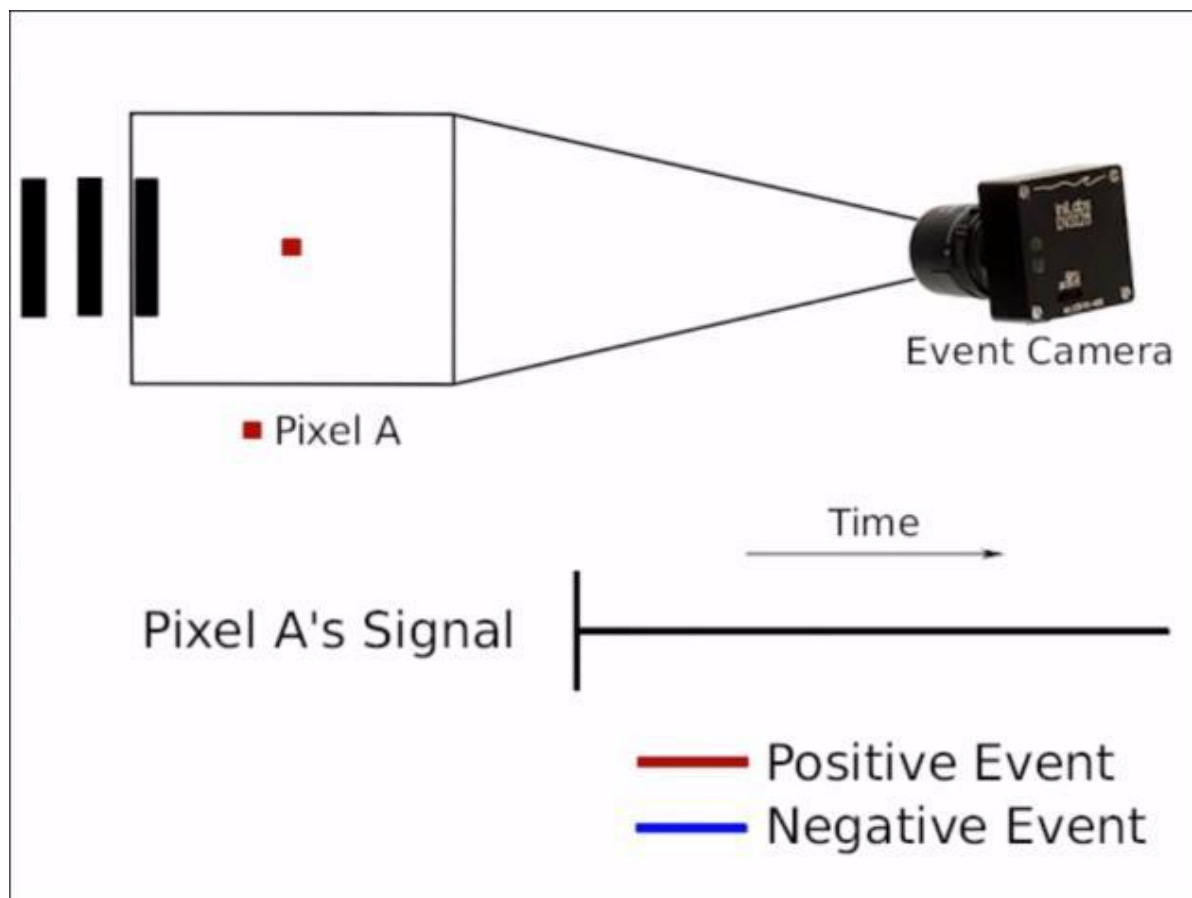
- Introduction to event cameras
- Semi-dense 3D structure estimation [1]
- Optical flow and intensity estimation [2]

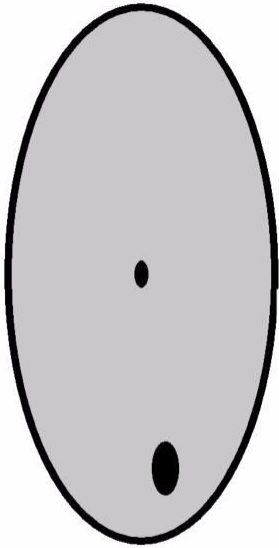
[1] H Rebecq, G. Gallego and D. Scaramuzza. “EMVS: Event-based Multi-View Stereo”, BMVC 2016.

[2] P. Bardow, A.J. Davison and S. Leutenegger. “Simultaneous Optical Flow and Intensity Estimation from an Event Camera”, CVPR 2016.

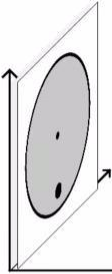
# Event cameras

- Silicon retina
- Pixel-level changes
- Asynchronous events (microsecond resolution)
  - OFF events – encode decreasing brightness
  - ON events – encode increasing brightness
  
- DVS – Dynamic Vision Sensor

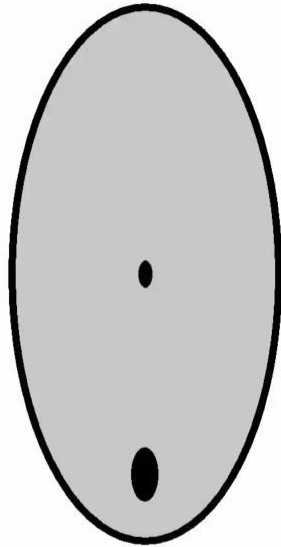




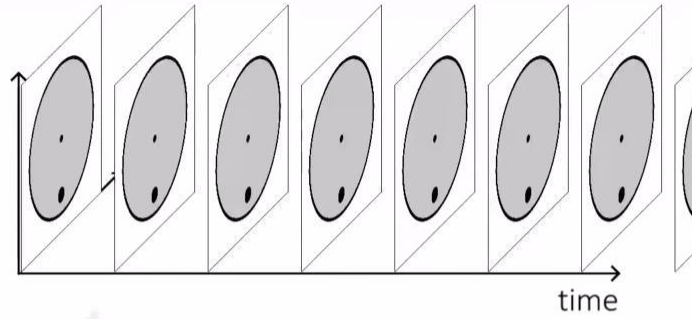
**standard  
camera  
output:**



time



**standard  
camera  
output:**

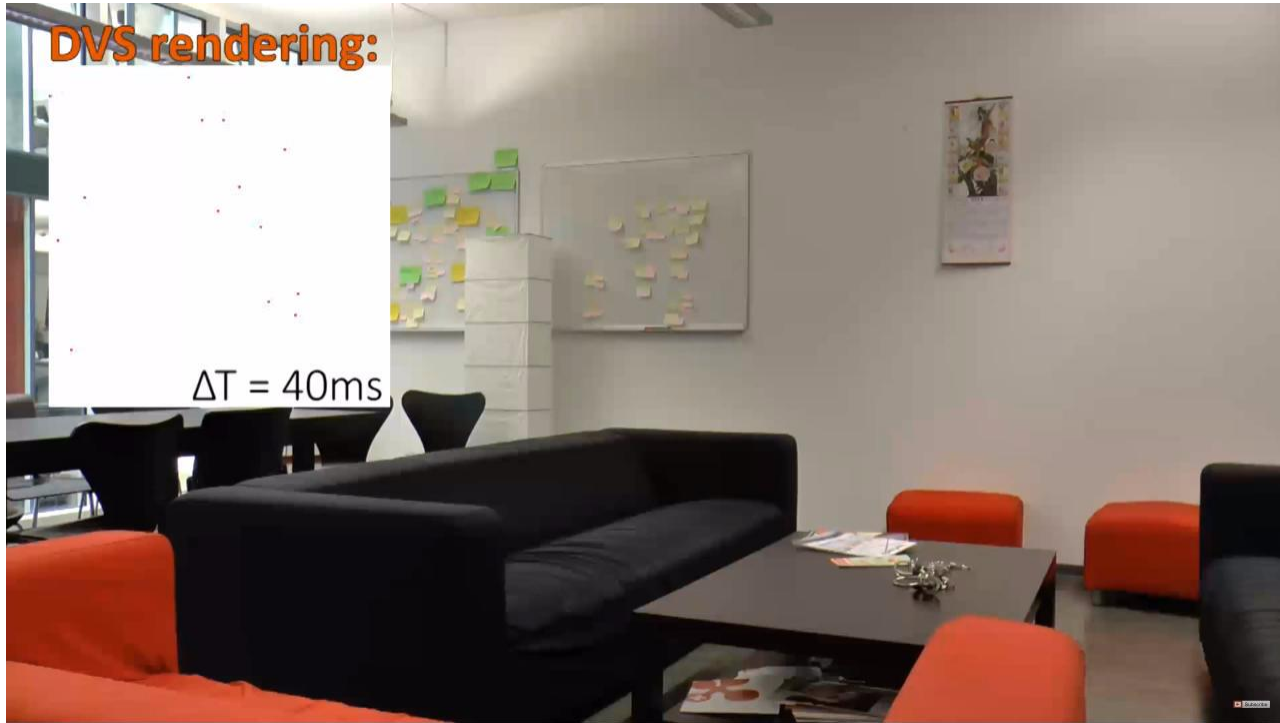


**DVS  
output:**



DVS rendering:

$\Delta T = 40\text{ms}$



# DVS

- No redundant information
- Low latency
- High dynamic range
- No motion blur
- Reduced power consumption
  
- Paradigm shift



- DVS128

**(Dynamic Vision Sensor)**

array size	128 x 128
pixel size	40 x 40 $\mu\text{m}$
dynamic range	120 dB
latency	15 $\mu\text{s}$
bandwidth	1 M events / sec
price	3000 CHF



[3] P.Lichtsteiner, C. Posch and T. Delbruck. "A 128x128 120dB 15 $\mu\text{s}$  latency asynchronous temporal contrast vision sensor". JSSC 2008

<http://inilabs.com/>

- **DAVIS240**  
**(Dynamic and Active-pixel Vision Sensor)**

array size	240 x 180
pixel size	18.5 x 18.5 $\mu\text{m}$
dynamic range	130 dB
latency	3 $\mu\text{s}$
bandwidth	3 M events / sec
ASP(active pixel sensor)	55 dB, 30 fps

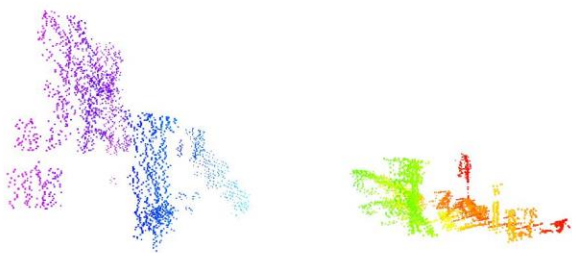


[4] C. Brandli, R. Berner, M. Yang, S.C. Liu and T. Delbruck. "A 240x180 130dB 3 $\mu\text{s}$  Latency Global Shutter Spatiotemporal Vision Sensor". JSSC 2014

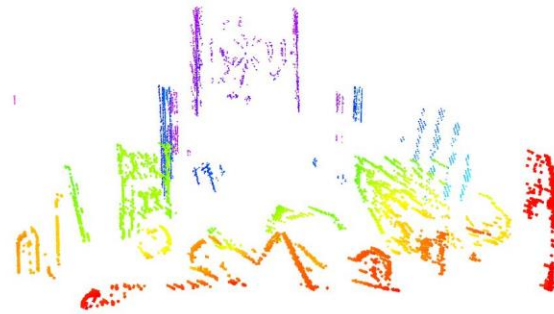
<http://inilabs.com/>

# EMVS: Event-based Multi-View Stereo [1]

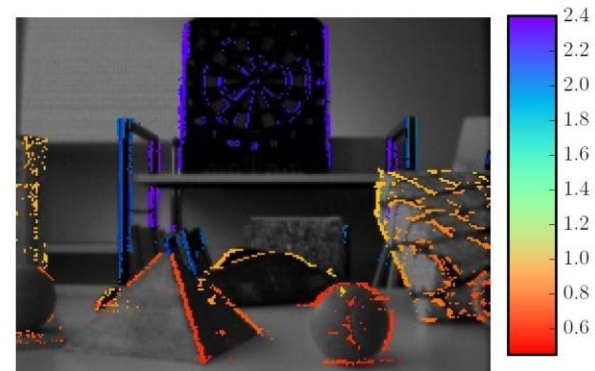
- Semi-dense 3D structure



(a) Side view.



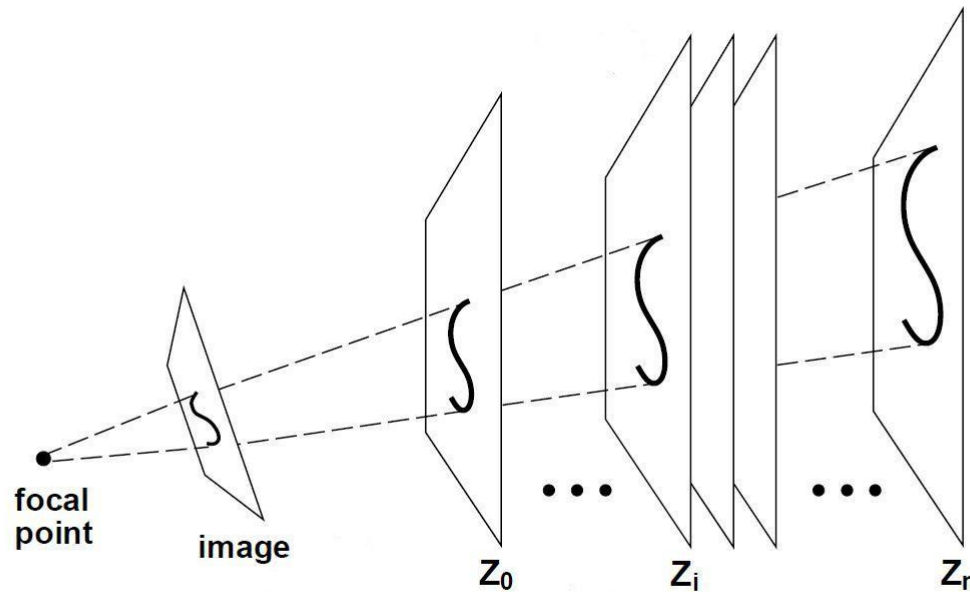
(b) Front view.



(c) Projection on a frame.

- **MVS** — the problem of 3D structure estimation, of a static scene, from a collection of images taken from known viewpoints

# A Space-Sweep Approach to True Multi-Image Matching [5]

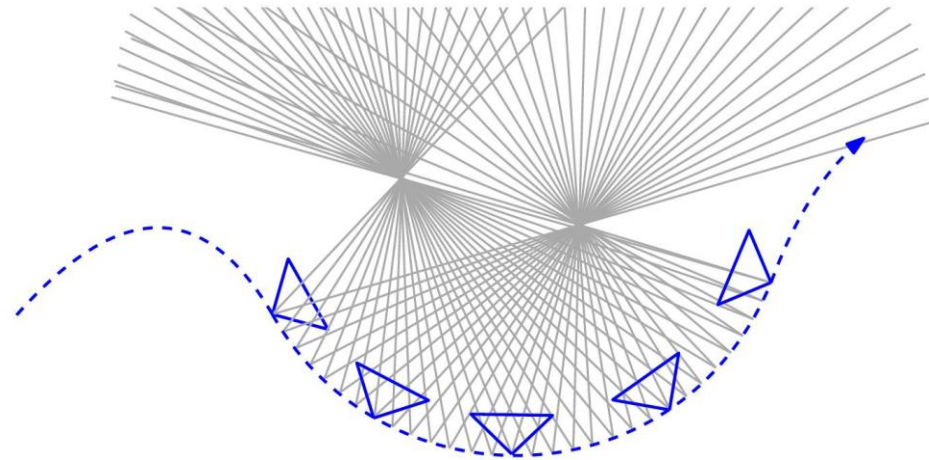
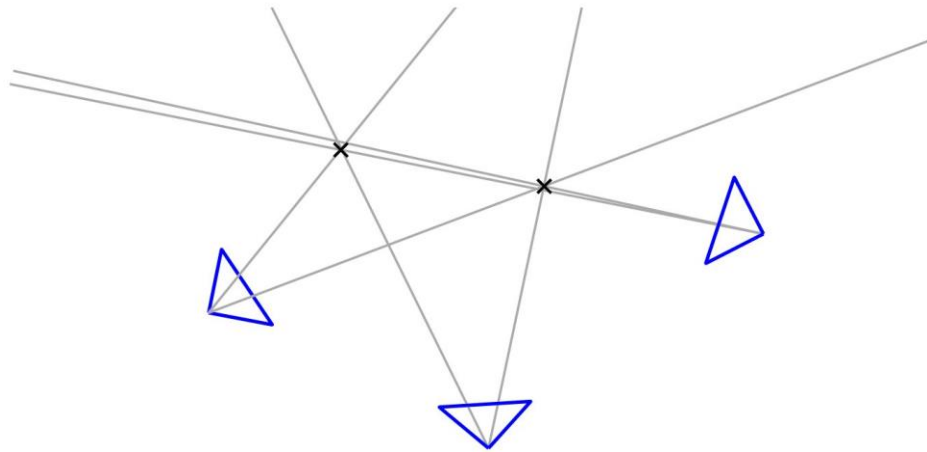


- Binary edge images

# Event-based Space-Sweep

1. Back-project event locations as rays through a defined volume of interest
2. Record the number of rays that pass through each voxel
3. Determine locations of 3D points

# Frame-based vs. Event-based



# Volume of interest - Disparity Space Image (DSI)

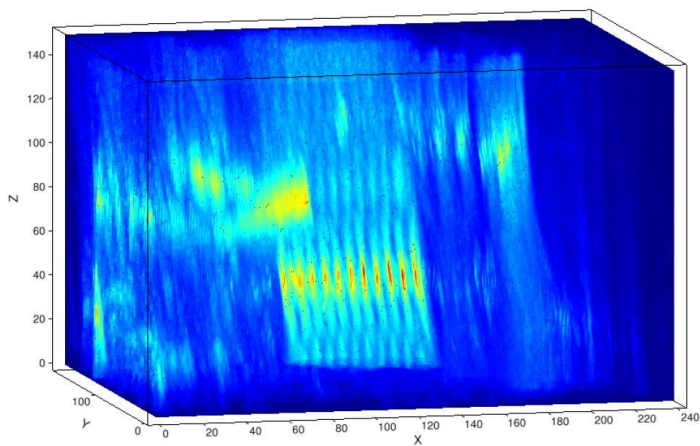


(240x180 px)

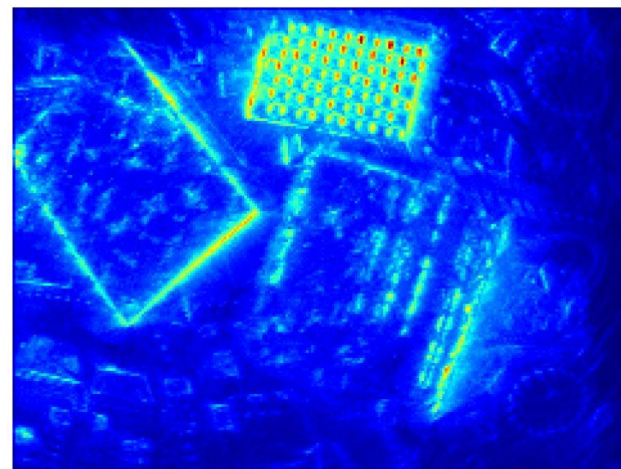


240 x 180 x 100 voxels

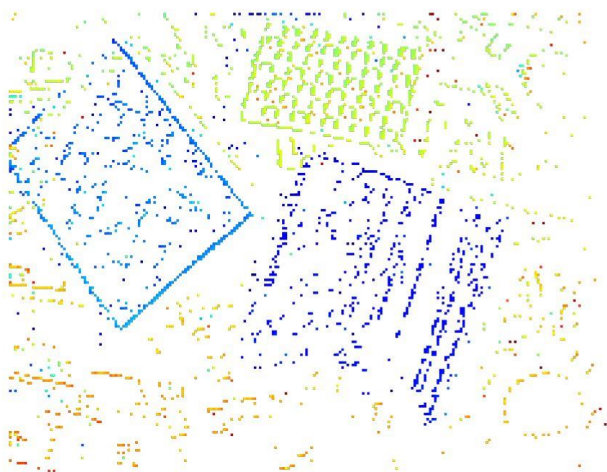




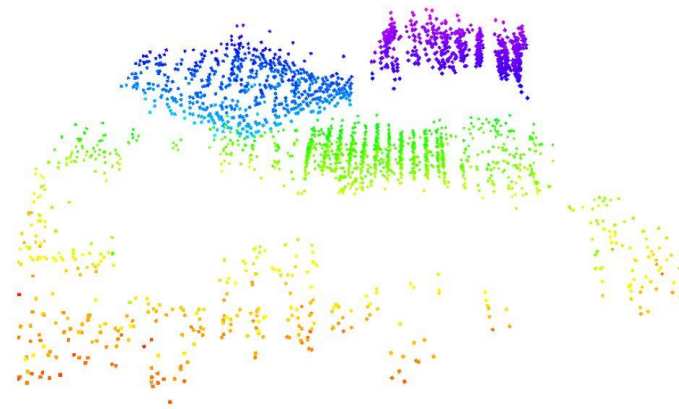
(a) Ray density DSI  $f(\mathbf{X})$ .



(b) Confidence map.



(c) Semi-dense depth map.



(d) 3D point cloud.



# Camera positions

- Motorized linear slider
- Visual odometry algorithm – SVO [6]

[6] C. Forster, M. Pizzoli and D. Scaramuzza. "SVO: Fast semi-direct monocular visual odometry". ICRA 2014

Table 1: Depth estimation accuracy in the synthetic datasets ( $N_z = 100$ )

	Dunes	3 planes	3 walls
Depth range	3.00 m	1.30 m	7.60 m
Mean error	0.14 m	0.15 m	0.52 m
Relative error	4.63%	11.31%	6.86%

Table 2: Depth estimation accuracy in the HDR experiment

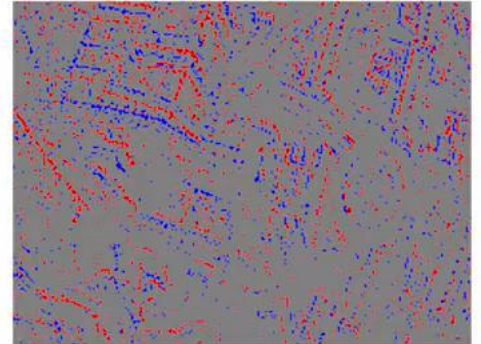
	Close (distance: 23.1 cm)		Far (distance: 58.5 cm)	
Illumination	Mean error	Relative error	Mean error	Relative error
○ constant	1.22 cm	5.29%	2.01 cm	4.33%
○ HDR	1.21 cm	5.25%	1.87 cm	3.44%

# Large-scale reconstruction with hand-held DAVIS

Frames (240x180 px)

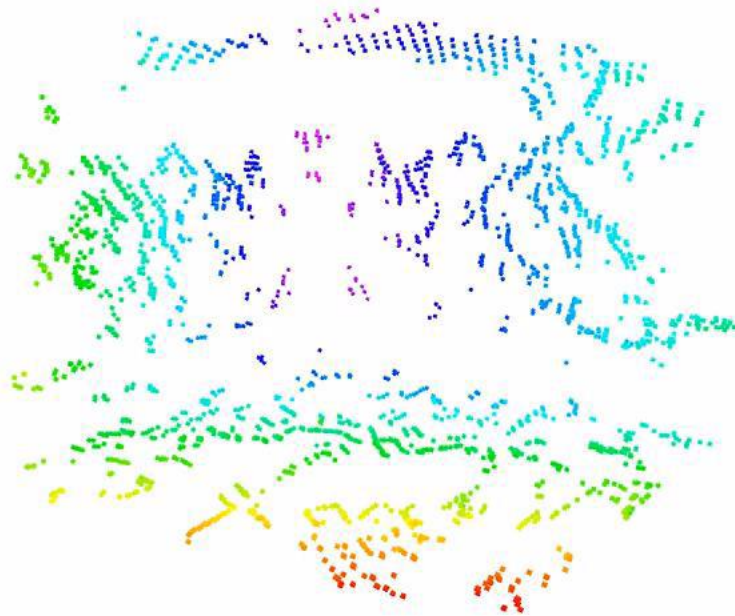


Events (ON, OFF)

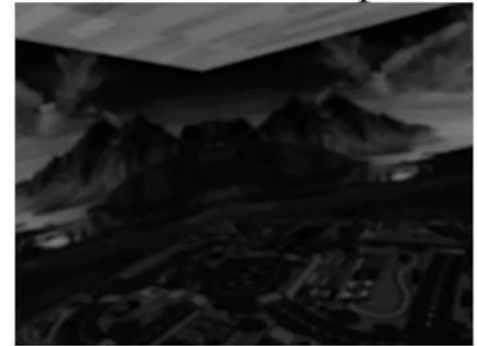


Real-Time

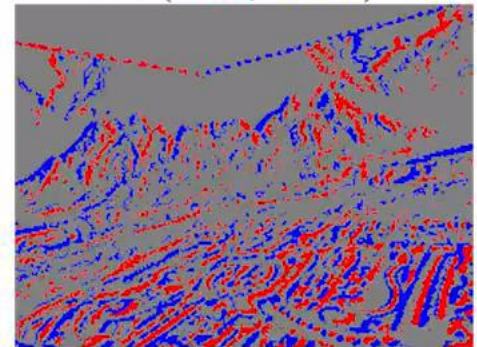
## 3 walls dataset (synthetic)



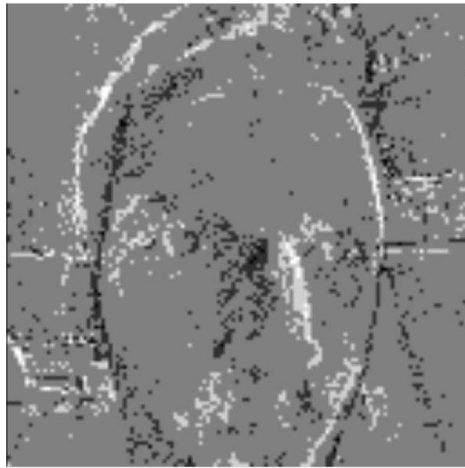
Frames (240x180 px)



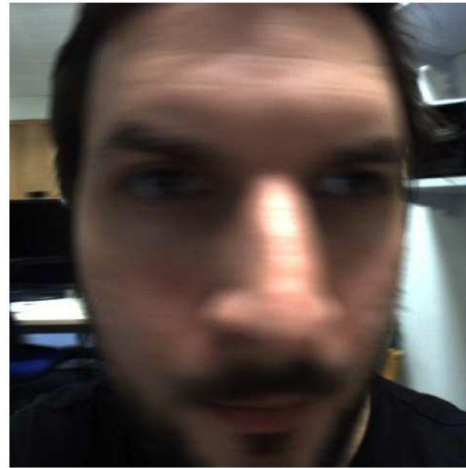
Events (ON, OFF)



# Simultaneous Optical Flow and Intensity Estimation from an Event Camera[2]



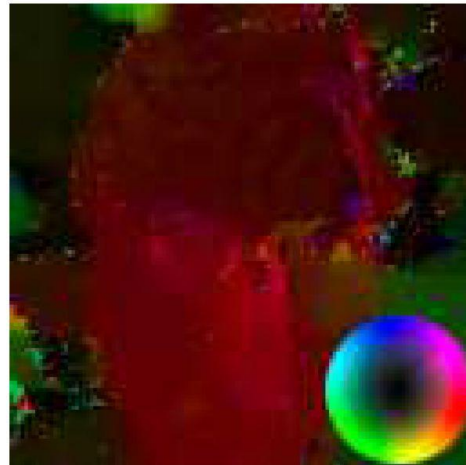
(a) Raw event camera output



(b) Standard camera image



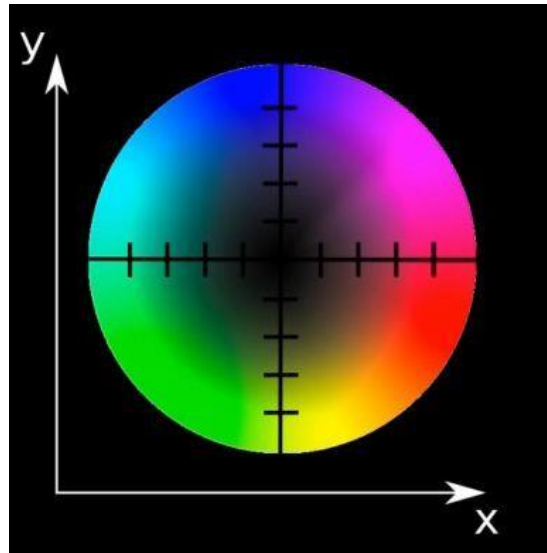
(c) Intensity estimate from events



(d) Optical flow from events

# Optical flow

- Apparent motion of brightness patterns



# Problem formulation

Events:  $e_i = (x_i, t_i, \rho_i)$

$x_i \in \Omega$	- position of the event
$t_i$	- timestamp
$\rho_i \in \{-1, 1\}$	- polarity

Event fired if:  $\left| L(x, t) - L(x, t_p(x, t)) \right| \geq \theta$

$L(x, t)$  log intensity at pixel  $x$ , at time  $t$   
 $t_p(x, t)$  time of the previous event

Goal:  $u$  - velocity  
 $I$  - image

Brightness constancy:  $I(x + \delta_t u, t + \delta_t) = I(x, t)$   $\delta_t$  time discretisation

Spatial smoothness of the flow

$$\lambda_1 \|u_x\|_1$$

Temporal smoothness of the flow

$$\lambda_2 \|u_t\|_1$$

Intensity smoothness

$$\lambda_3 \|L_x\|_1$$

Temporal consistency

$$\lambda_4 \| \langle L_x, \delta_t u \rangle + L_t \|_1$$

Event data term

$$\sum_{i=2}^{P(x)} \|L(x, t_i) - L(x, t_{i-1}) - \theta \rho_i\|_1$$

$P(x)$  set of all events fired at  $x$

No-event data term

$$\lambda_5 h_\theta \left( L(x, t) - L(x, t_p(x, t)) \right)$$

$$h_\theta(x) = \begin{cases} |x| - \theta & , \text{if } |x| > \theta \\ 0 & , \text{otherwise} \end{cases}$$

Prior image constraint

$$\|L(x, t_1) - \hat{L}(x)\|_2^2 \quad \hat{L} - \text{prior image}$$

$t_1$  - first event timestamp at  $x$ , in current window, or minimum of  $T$



# Discretisation

$\Omega \Rightarrow$  regular pixel grid of size  $M \times N$

$T \Rightarrow K$  cells, each of length  $\delta_t \mu s$

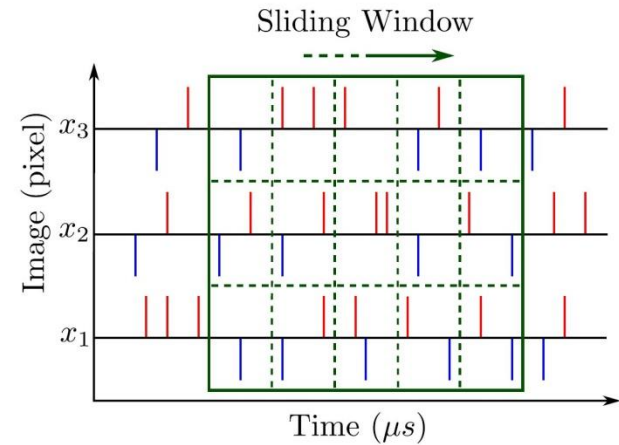


Figure 3: The sliding window (green box) bins the incoming positive events (red bars) and negative events (blue bars) into a regular grid (dashed lines). When the minimisation converges, the window is shifted to the right.

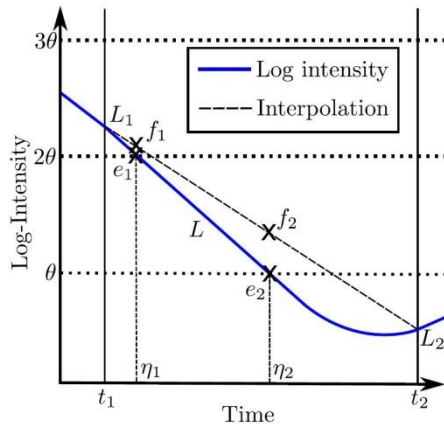


Figure 4: Approximation of the intensity for two given events  $e_1$  and  $e_2$  between two intensity estimates  $L_1$  and  $L_2$ . For the discrete data term, we use the linear approximations  $f_1$  and  $f_2$  at the time of each event  $\eta_1$  and  $\eta_2$ .

# Optimisation

$$\min_{u,L} \int_{\Omega} \int_T \left( \lambda_1 \|u_x\|_1 + \lambda_2 \|u_t\|_1 + \lambda_3 \|L_x\|_1 + \lambda_4 \|\langle L_x, \delta_t u \rangle + L_t\|_1 + \lambda_5 h_{\theta} (L - L(t_p)) \right) dt dx$$
$$+ \int_{\Omega} \left( \left( \sum_{i=2}^{|\mathcal{P}(x)|} \|L(t_i) - L(t_{i-1}) - \theta \rho_i\|_1 \right) + \lambda_6 \|L(x, t_1) - \hat{L}(x)\|_2^2 \right) dx$$

- preconditioned primal-dual algorithm [7]
- Legendre-Fenchel transform [8]

[7] T.Pock and A. Chambolle. "Diagonal preconditioning for first order primal-dual algorithms in convex optimization". ICCV 2011

[8] A. Handa, R. A. Newcombe, A. Angeli and A.J. Davison. "Applications of the Legendre-Fenchel transformation to computer vision problems"

# Experiments

DVS128 => 128 x 128

$K = 128, \delta_t = 15\text{ms}$

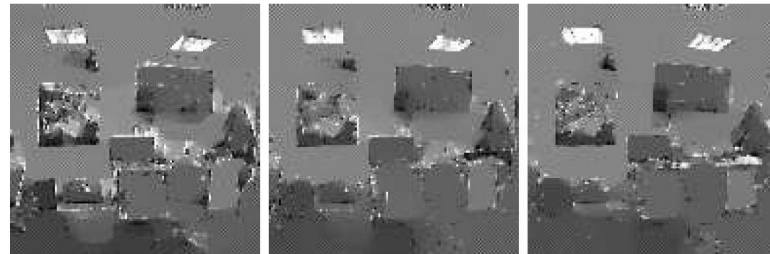
$\theta = 0.22$

$\lambda_1 = 0.02, \lambda_2 = 0.05, \lambda_3 = 0.02, \lambda_4 = 0.2, \lambda_5 = 0.1, \lambda_6 = 1$

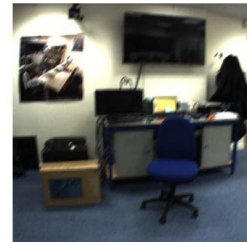
- Benefits of simultaneous estimation



(a) Without optical flow



(b) With optical flow



(c) Camera images

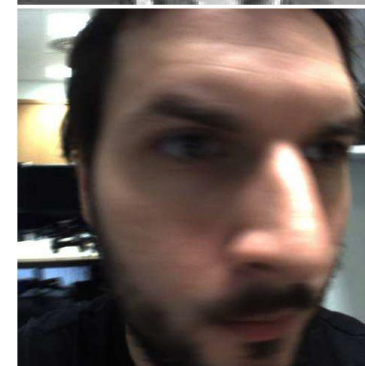
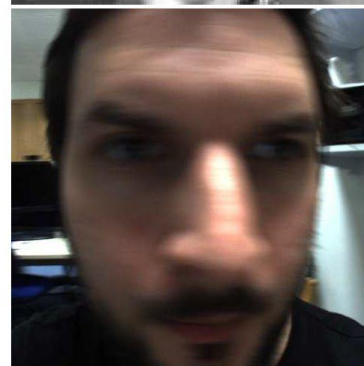
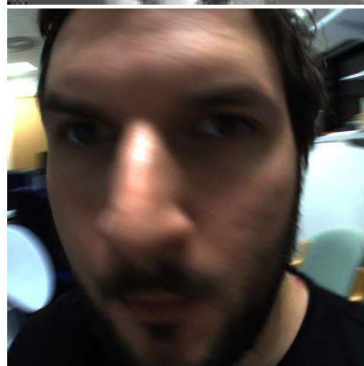
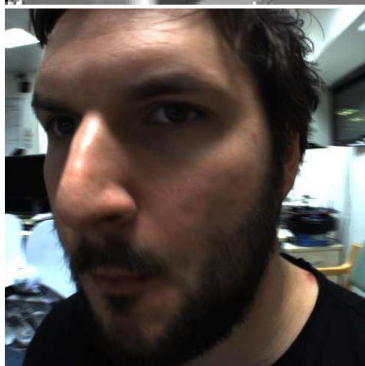
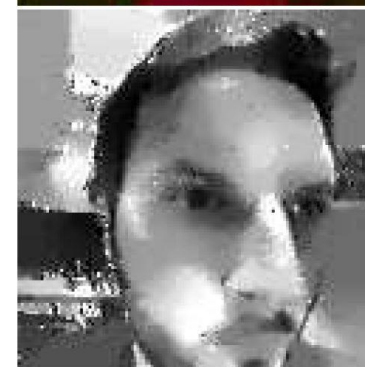
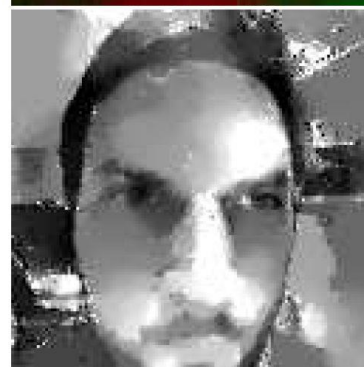
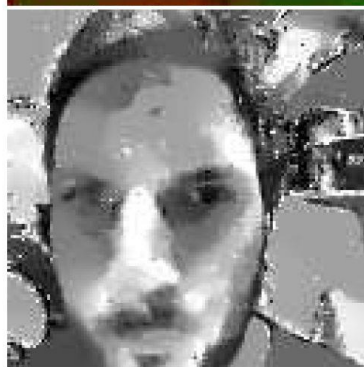
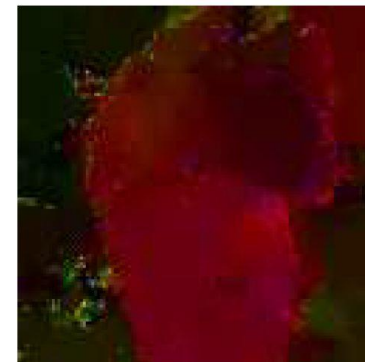
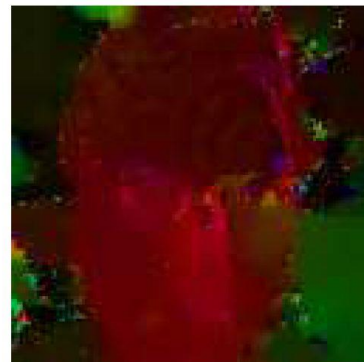
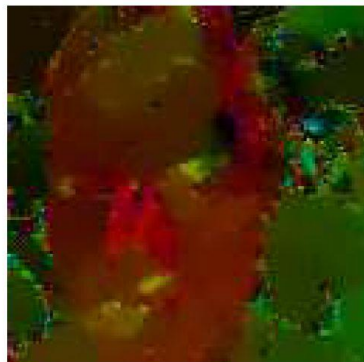
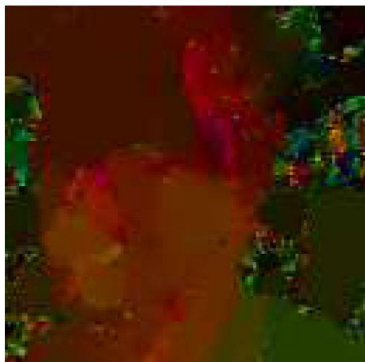
# Experiments

DVS128 => 128 x 128

$K = 128, \delta_t = 15\text{ms}$

$\theta = 0.22$

$\lambda_1 = 0.02, \lambda_2 = 0.05, \lambda_3 = 0.02, \lambda_4 = 0.2, \lambda_5 = 0.1, \lambda_6 = 1$



# Experiments

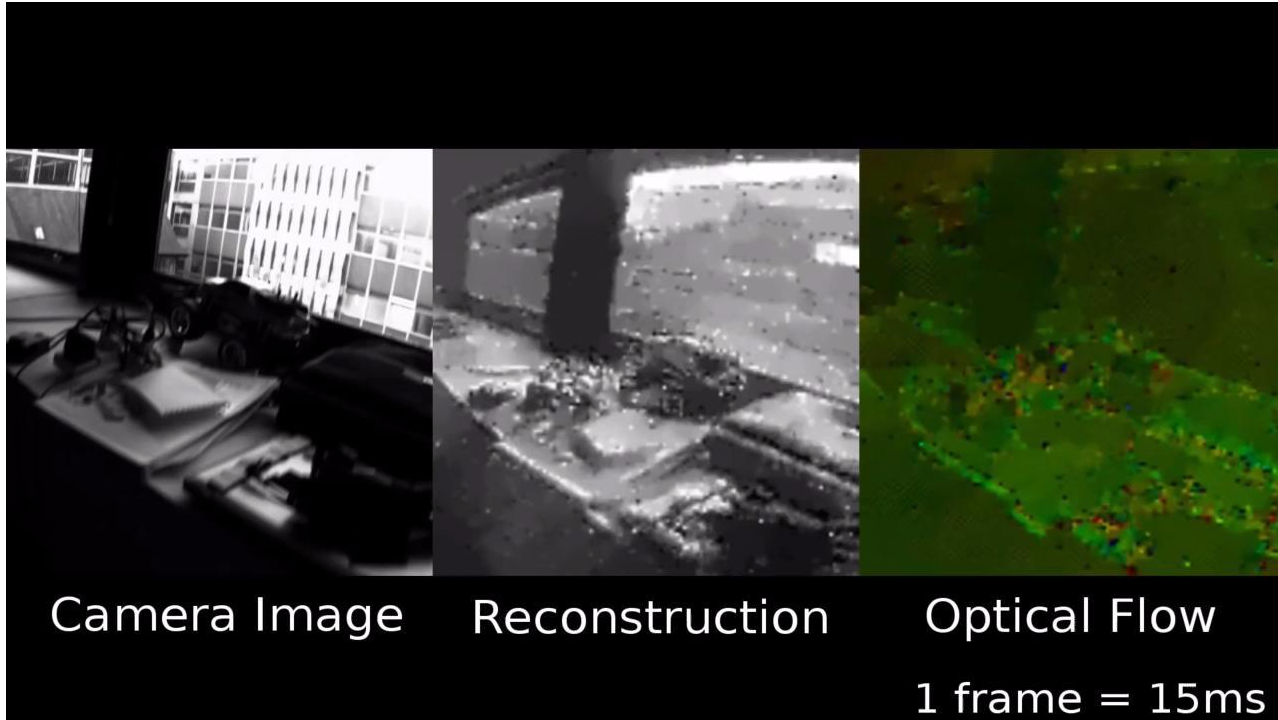
DVS128 => 128 x 128

$K = 128, \delta_t = 15\text{ms}$

$\theta = 0.22$

$\lambda_1 = 0.02, \lambda_2 = 0.05, \lambda_3 = 0.02, \lambda_4 = 0.2, \lambda_5 = 0.1, \lambda_6 = 1$

- High Dynamic Range





# Experiments

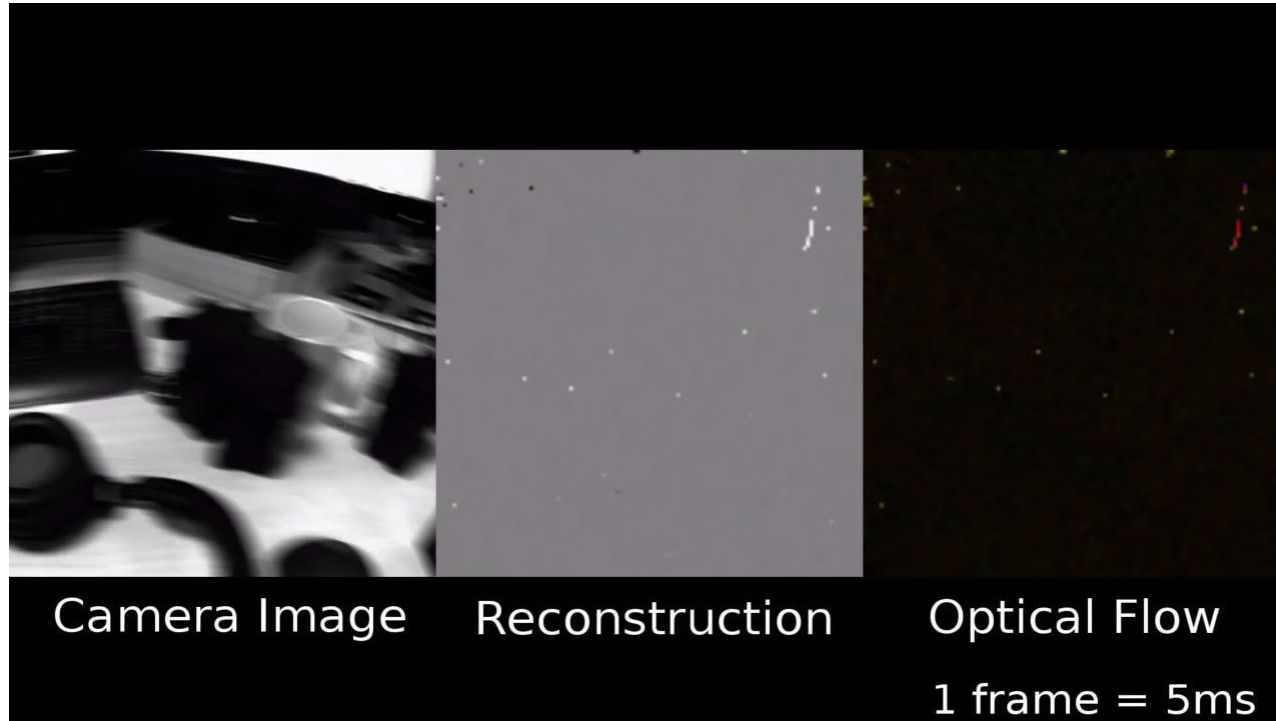
DVS128 => 128 x 128

$K = 128$ ,  $\delta_t = 4\text{ms}$

$\theta = 0.22$

$\lambda_1 = 0.02$ ,  $\lambda_2 = 0.05$ ,  $\lambda_3 = 0.02$ ,  $\lambda_4 = 0.2$ ,  $\lambda_5 = 0.1$ ,  $\lambda_6 = 1$

- Rapid motion



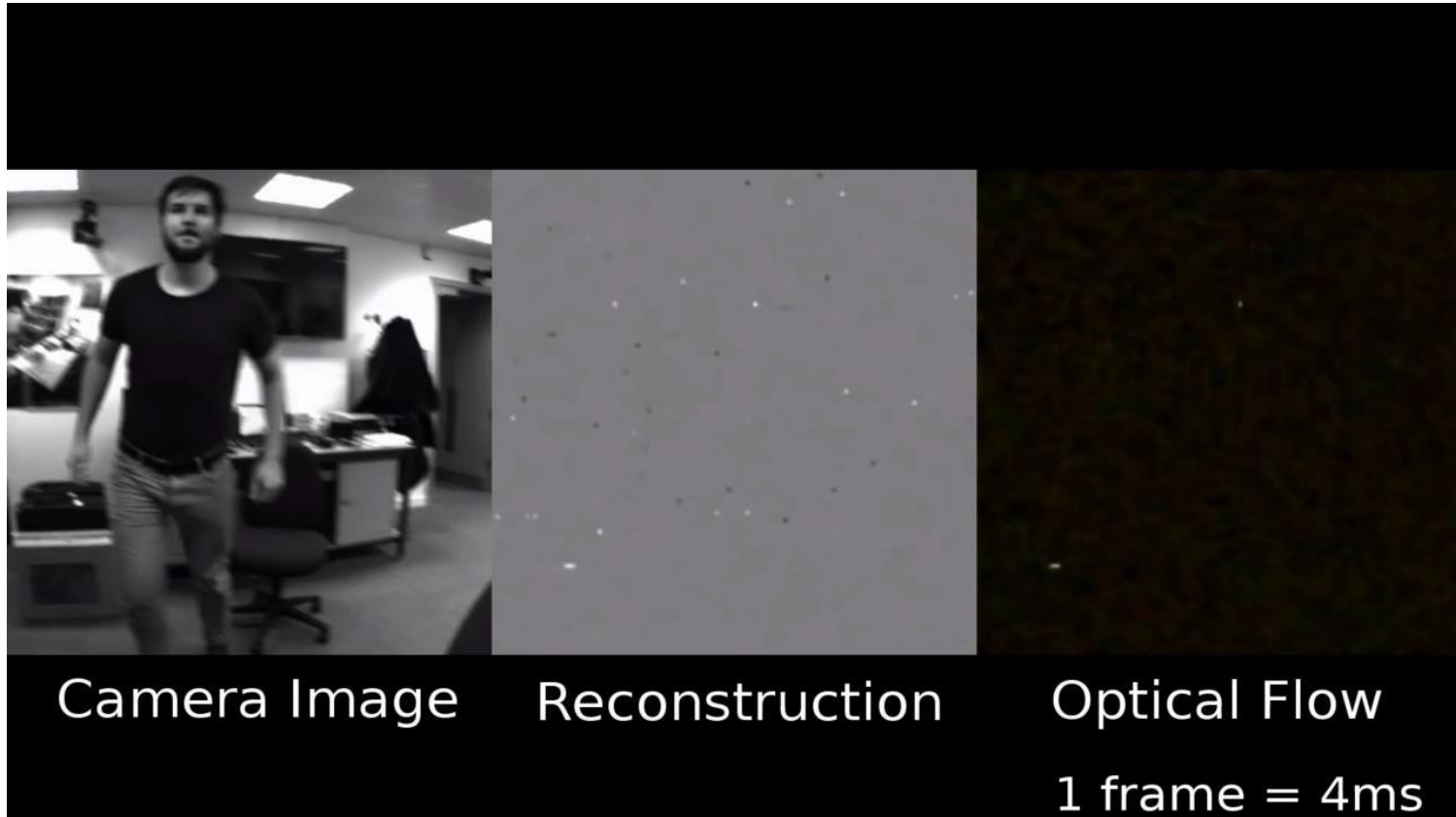
# Experiments

DVS128 => 128 x 128

$K = 128$ ,  $\delta_t = 7\text{ms}$

$\theta = 0.22$

$\lambda_1 = 0.01$ ,  $\lambda_2 = 0.05$ ,  $\lambda_3 = 0.01$ ,  $\lambda_4 = 0.2$ ,  $\lambda_5 = 0.1$ ,  $\lambda_6 = 1$



# References

- [1] H Rebecq, G. Gallego and D. Scaramuzza. “EMVS: Event-based Multi-View Stereo”, BMVC 2016
- [2] P. Bardow, A.J. Davison and S. Leutenegger. “Simultaneous Optical Flow and Intensity Estimation from an Event Camera”, CVPR 2016
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- [5] R.T. Collins. “A space-sweep approach to true multi-image matching”. CVPR 1996
- [6] C. Forster, M. Pizzoli and D. Scaramuzza. “SVO: Fast semi-direct monocular visual odometry”. ICRA 2014
- [7] T.Pock and A. Chambolle. “Diagonal preconditioning for first order primal-dual algorithms in convex optimization”. ICCV 2011
- [8] A. Handa, R. A. Newcombe, A. Angeli and A.J. Davison. “Applications of the Legendre-Fenchel transformation to computer vision problems”